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Nuclear magnetic resonance and spin relaxation in biological systems[™] Robert G. Bryant^{a,*}, Jean-Pierre Korb^b

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Abstract

Proton nuclear spin-lattice relaxation in biological systems is generally distinguished from that in inorganic systems such as rocks by the presence of locally disordered macromolecular environments. Rapid exchange of readily observed labile small molecules among differently oriented macromolecular sites generally nearly averages the spectral anisotropies in the small molecule resonances. The biological tissue is generally distinguished from the inorganic matrix by the presence of a significant population of protons in the solid components that are well connected by dipolar spin couplings. Magnetic coupling between the solid and the liquid components generally described by a power law in the Larmor frequency. Recent theory involving a modification of the spin-phonon class of relaxation mechanism provides a quantitative understanding of these data in terms of the dynamics of the chain molecules generally present in the solid spin systems, folded proteins for example.

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1. Magnetic features of boilogical systems

If we divide materials into biological and nonbiological porous systems, nuclear magnetic resonance and spin relaxation in biological systems have both important similarities as well as important differences from other microporous materials. Like inorganic systems such as zeolites, clays, rocks and porous glasses, the biological systems may present a variety of locally ordered environments that provide dynamic constraints on the trajectories of mobile molecules. The biological systems are generally composed of a relatively extensive but soft matrix of molecules that are solid in the sense that they do not rotate freely, but are soft in that there may be considerable range of internal motion possible, and the biological systems are usually deformable on a macroscopic scale. The inorganic matrix on the other hand is often macroscopically porous, but the matrix is sufficiently cross-linked that the structural support provided to the mobile and readily observed entrapped molecules is rigid and not deformable. An important feature for relaxation is that the natural inorganic

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systems are often contaminated by considerable paramagnetic ion impurities as both surface bound ions and matrix substitutions in the rigid support. Paramagnetic centers are, of course, present in biological systems as well, but are often well sequestered by macromolecules as in the metalloproteins. Freely diffusing inorganic ions such as iron(II), iron(III) or manganese(II) are rare and do not often contribute to the predominate relaxation pathways except in special circumstances such as blood. Both classes of system may provide considerable short range and sometimes long range organization to observed molecules that may affect the spin relaxation by changing the effective dimensionality of the space sampled by the dynamics of the observed spins. The effects of such local order may change the magnetic field dependence of the spin-lattice relaxation rate dramatically.

An often crucial distinction between inorganic and biological systems is that the inorganic system is often proton-poor; that is, the solid matrix is composed of structures that do not include a well-connected proton spin network. In this case the proton spin relaxation of the observed liquid component, and the magnetic field dependence in particular, may reflect the character of the constrained diffusive processes that drive relaxation. In the majority of biological systems the confining structures are proton-rich; the protons then form a major population of

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strongly coupled spins that may interact with readily observed spins mobile with which they are in intimate contact. The presence of the large, but generally unobserved solid proton population in a biological sample such as a tissue may have dominant effects on the proton spin relaxation of the observed species including the solvent and a variety of small molecules that may be of metabolic or therapeutic interest. We focus in this discussion on the biological systems and several features of the spin-lattice relaxation processes.

2. Anisotropy

A distinguishing feature of NMR in immobilized systems is that all anisotropies in the system may appear; that is, the chemical shift anisotropy, nuclear electric quadrupole couplings and dipolar couplings are not averaged by rapid rotational motions. One might expect that the spectroscopy of biological systems would then be dominated by the richness of such anisotropic interactions; however, this is usually not the case if low-molecular-weight components are observed. Although biological systems may be locally ordered, it is rare that the systems are uniformly oriented at the molecular level. Fig. 1 represents a cartoon of biological solids that are compositionally identical, but where the local order is different. Both systems are solid and no rotational averaging is observed in the solid components, direct observation of which would reveal the usual solid-state powder pattern spectra showing the usual dipolar, quadrupolar or chemical shift anisotropies. More generally one observes the small molecules because of dramatically increased sensitivity and possibly resolution. In this case, the spectrum, even of a quadrupolar nucleus such as ³⁵Cl or ²H, does not reveal directly the anisotropy of the semisolid system even when the observed spin may reside on a molecule that may bind and exchange with unique binding sites on the solid matrix of molecules. Generally, a broadened Lorentzian line is detected with a narrow central portion and a broader than normal spectral wings as shown in Fig. 1A. This spectrum is essentially rotationally averaged by chemical exchange of the observed small molecule between locally ordered binding sites of different orientation in the magnetic field. In a cross-linked protein, for example, the exchanging spin may sample several hundred sites in the time of a spectral acquisition time, which nearly averages the anisotropy of the sites sampled. Each bound site corresponds to a particular line or pair of lines in the powder pattern, but the next site corresponds to a position in the powder pattern; when several hundred such sites are sampled by each observed molecule, the spectrum collapses as in other rapid chemical exchange cases. However, the solid effects may persist in some ways because the anisotropic interactions are not completely averaged by the exchange processes. Thus, spins such as ³⁵Cl or ²³Na ion may often pass multiple quantum filters that a species that never samples a bound anisotropic site does not [1-10].

A distinctly different spectrum results when the local environment is uniformly oriented in the magnetic field as in a crystal, which is shown schematically in Fig. 1B. In this case, exchange of the observed and labile species with these sites averages the spectrum of the isotropic phase with that of the ordered solid phase to an average position. When different locally ordered domains are summed as in a polycrystalline sample, then the result is a powder pattern



Fig. 1. (A) The ³⁵Cl NMR spectrum of cross-linked serum albumin containing mercury(II) at sulfhydryl sites that provide a strongly bound though rare site for exchange of chloride ion. The detected NMR spectrum in the bulk chloride ion resonance is a super Lorentzian line where the effects of the anisotropy of the bound environment are lost. (B) The ²H NMR spectrum of a phenyl propionic acid in cross-linked crystals of the carboxypeptidase A; the exchange of the phenyl propionic acid with the uniformly oriented binding sites preserves the line shape of the solid environment even though the ligand reorients uniformly in the unbound phase [12].



Fig. 2. A computed representative free induction decay of magnetization in a dynamically heterogeneous system such as a tissue containing both solid and liquid components with drastically different values for the transverse relaxation rate.

where the width is scaled by the ratio of the concentration of the bound anisotropic population to that unbound and isotropic phase. In the case shown, the deuterium in an inhibitor exchanges with the active site of carboxypeptidase A in a cross-linked crystal and the spectrum is a scaled powder pattern from which the usual deuterium line shape analysis may be extracted [11,12]. Biological tissues usually do not provide the high degree of local order found in a crystal and spectra like that shown in Fig. 1A are observed. However, important and useful exceptions occur in highly ordered systems where intramolecular dipolar couplings are preserved in the water resonances [7].

3. Relaxation coupling

Although usually not observed in MRI measurements, both the solid and liquid components of biological systems may be detected as shown in Fig. 2. In the time domain, the solid components appear only in the earliest part of the free induction decay often with transverse relaxation time constants in the range of tens of microseconds. It is useful to note that the frequency domain presentation of the same data presents a major dynamic range problem in that the line width of the solid component is usually more than a thousand times wider that that of the liquid or small molecule components; thus, its amplitude at the maximum is approximately a thousand times smaller that that of the liquid even if the two spins are present at the same concentration. Thus, the solid is generally not observed in the Fourier transformed spectrum when the liquid components are displayed and the problem may be seriously aggravated if the spectrometer has a dead time the order of or longer than the short T2 of the solid signal. The simultaneous detection of liquid and solid components has important practical applications; an example is application to the solid fat index in the food industry [13,14].

In most dynamically heterogeneous biological systems such as tissues, a consequence of the solid components is that the nuclear spin relaxation rate constants of the small molecule spins are affected by magnetic coupling to the solid spins. This spin coupling is often a dominant factor in the proton spin-lattice relaxation. A simple demonstration of the coupling is that following a selective pulse, the magnetization of one population pumps that in the second until the magnetizations equilibrate, then they relax together with a composite rate constant that is given by the roots of the coupled differential relaxation equations as shown in Fig. 3 [15,16]. Thus, it is not appropriate to measure longitudinal magnetization relaxation in a tissue and call the apparent decay constant a T_1 value appropriate to the small molecule measured, water for example, and apply simple relaxation equations to interpret such values.

An interesting application of the coupled relaxation is indirect detection of the solid component spectrum, which is generally tens of kHz wide. Because the spin populations are coupled, perturbation of one population affects the other. A simple implementation is to irradiate the solid component with a preparation pulse that is at a frequency different from the dominant solvent resonance and then detect the amplitude of the solvent proton resonances as a function of the preparation pulse irradiation frequency. An example is shown in Fig. 4 where the effects on three solvent components are detected simultaneously, water, acetone and dimethyl sulfide in a cross-linked serum albumin gel that models tissue approximately. The detailed shape of the resulting solid component spectrum is a function of the strength of the irradiating preparation pulse and the line shape is susceptible to broadening by saturation effects as in continuous wave spectroscopy [17]; however, it is clear in Fig. 4 that the protons of all three solvent components suffer a cross-relaxation with the immobile protein protons. The efficiency of the coupling is different as shown by the different amplitudes in the cross-relaxation spectrum, which is most strongly related to the number of



Fig. 3. The response of water and protein proton populations as a function of time following a selective excitation of the water spins. At long times, the two populations decay at identical rates as predicted [64].



Fig. 4. The proton NMR spectrum of the protein detected by off-resonance irradiation of the protein protons in a cross-linked protein gel containing three solvents: acetone, dimethyl sulfide, and water. The effects of relaxation coupling are apparent in all three solvent resonances [19].

binding sites for the small molecules on the protein [18,19]. The effects of such coupling are general and depend on the dipole–dipole interactions, which have been discussed in detail [20-23]. We point out only that these relaxation coupling effects will be present in the spectra of most proton-containing molecules observed in vivo spectroscopic or imaging experiments.

The magnetic coupling may affect dramatically the magnetic field dependence of the spin-lattice relaxation rates as shown in Fig. 5 where residual water protons are observed in D_2O suspensions of phosphatidyl choline large unilamellar vesicles. By itself, the relaxation rates of the water protons are independent of the magnetic field strength

because all of the motions that modulate magnetic couplings are at frequencies much higher than the frequencies utilized in the experiments of Fig. 5. The magnetic field dependence results from a weak coupling between the water protons and the lipid protons [24-33] which transfers the lipid proton dispersion profile to the water protons. Thus, the water proton system may be utilized to characterize the molecular dynamics of the lipid system, which may be described by several complex dynamical models appropriate to chain molecules [34-38].

4. Comprehensive relaxation model

The magnetic field dependence of the water proton spinlattice relaxation in tissues as well as simpler rotationally immobilized protein systems is described by a power law in the Larmor frequency [39-46] with the exponent typically between 0.5 and 0.8. For a protein solution, the MRD is a Lorentzian dispersion where the inflection point reports the rotational correlation time for the protein reorientating by rotational Brownian motion [47-50]. If the protein rotational motions are stopped by chemical cross-linking at essentially constant composition [39,51], the MRD profile changes from the Lorentzian to a power law as shown in Fig. 6 [39,51]. In both cases, the water proton spin-lattice relaxation rate constant is determined by coupling to the protein protons. The efficiency of the coupling is dominated by exchange of whole water molecules with specific sites on or in the protein where cross-relaxation with the protein protons is efficient. In the solid, the coupling in the bound state is particularly efficient because the bound water molecule is essentially a solid and the cross-relaxation rate



Fig. 5. The magnetic relaxation dispersion profile for residual water protons in D_2O suspensions of large unimellar phosphatidyl choline vesicles at 40 mM and 296 K (K. Victor, R.G. Bryant, unpublished data). The inset is based on data reported by Rommel et al. [66].

constant is essentially the T_2 of the solid proton system or approximately 10 µs. In addition, proton exchange from a variety of labile proton positions on the protein may contribute to the total coupling. Although the tissue represents a complex superposition of contributions, the observed power law is the same and the total spin relaxation of the water protons responds to changes in the concentration of water as predicted by a quantitative treatment of the cross-relaxation coupling [39,51].

Although it has been known for some time that the water proton spins report the magnetic field dependence of the solid component protons, which are described by a power law, the physical origin of the power law has been only recently understood. Kimmich et al. measured the MRD of polypeptides and made the important observation that the power law was present in samples of polyglycine, which has no side chain protons; thus, they suggested that the power law derived from motions of the polypeptide backbone [52]. This idea has recently been put on quantitative foundation by detailed consideration of relaxation induced by spinphonon coupling [53-56].

The spin-phonon coupling in a three-dimensional crystal is very inefficient relaxation pathway as pointed out by Abragam [57]. However, there is a profound difference between a phonon in a three-dimensional crystal where the correlation of the local disturbance may be lost rapidly and a chain molecule in which the local disturbance may move in an effective space of dramatically reduced dimensionality provided by the chain molecule. In the folded protein, the strong connectivity is in the covalent connectivity provided by the chemical bonds of the polypeptide chain. Although the amino acid side chains are in van der Waals contact in many cases, these connections are weak so that the structural disturbance propagates primarily along the polypeptide chain. The effect of the reduced dimensionality is to increase the efficiency of the spin-phonon coupling by many orders of magnitude [53]. The detailed theory, presented elsewhere [54], provides a quantitative description of the spin-lattice relaxation rate of the protein components of a



Fig. 6. The water proton magnetic relaxation dispersion profile in 1.8 mM aqueous bovine serum albumin solution and the cross-linked serum albumin gel obtained at the same at the same composition at 298 K [39].



Fig. 7. Schematic representation of relaxation pathways for proton spin relaxation in heterogeneous protein systems that are models for tissues.

protein–water system when the protein is not free to rotate and the effects of the relaxation coupling are included in the complete model. This model accounts for the magnetic field and composition dependence of water and protein proton spin-lattice relaxation rate constants and provides a foundation for understanding the more complex tissue. The essence of the model is summarized in Fig. 7.

The protein proton spin-lattice relaxation is dominated by the structural fluctuations that propagate along the polypeptide chain and which modulate proton-proton dipole-dipole couplings. Motion anywhere relaxes the whole protein proton population because the protons in the rotationally immobilized protein are well coupled to each other, that is, spin diffusion within the protein system is rapid and the population may be said to achieve a common spin temperature in a short time, on the order of T_2 or 10 µs. The water protons are coupled to the protein protons by several magnetic exchange mechanisms, the dominant one being the exchange of whole water molecules with rare binding sites on the protein. The measured field dependence may be discussed in terms of three regions. (1) The region above approximately 10 MHz is dominated by high-frequency motions in the system such as water molecule rotation or methyl group rotation [58-64]. (2) The intermediate field region is dominated by the chain dynamics in the folded protein and displays the characteristic power law in the Larmor frequency. (3) The low field region may present a plateau that in turn may have two causes. (a) Limitations in the magnetization transfer rate between the protein and the water may provide a limitation on the low field rate constant for the water protons. (b) The local magnetic field sensed by protein protons is limited by the effective local dipolar field, which is approximately 11 kHz. Thus, although the applied dc magnetic field that is applied to the sample may be lower than 11 kHz, the effective field dependence of the spin-lattice relaxation rate is truncated by the dipolar field [65]. In summary, in the intermediate field regime, the water proton spin-lattice relaxation is tied to the structural fluctuations in the protein

which propagate primarily along the primary structure of the polypeptide chain.

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